

Spurious Precision in Meta-Analysis

(of Observational Research)

Z. Irsova¹ P. Bom² T. Havranek^{1,3} H. Rachinger⁴

¹Charles University, Prague

²University of Deusto, Bilbao

³Centre for Economic Policy Research, London

⁴University of the Balearic Islands, Palma

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Meta-Research Innovation Center at Stanford

In a nutshell

Main Message

- 1 Researchers may report artificially high precision.
- 2 Then standard meta-analysis methods fail.
- 3 Solution: Meta-Analysis Instrumental Variable Estimator (MAIVE).

Project Website

meta-analysis.cz/maive

STAR experiment: class size and learning

Table: Regression of individual test scores on class size

	(1)	(2)	(3)	(4)
Small class (treatment)	4.82 (2.19)	5.37 (1.26)	5.36 (1.21)	5.37 (1.19)
White/Asian			8.35 (1.35)	8.44 (1.36)
Girl			4.48 (0.63)	4.39 (0.63)
Free lunch			-13.15 (0.77)	-13.07 (0.77)
White teacher				-0.57 (2.1)
Teacher experience				0.26 (0.10)
Master's degree				-0.51 (1.06)
School intercepts	No	Yes	Yes	Yes
Sample	5,861	5,861	5,861	5,861

Notes: Adapted from Krueger (1999). Dependent variable: test score percentile.

Standard errors in parentheses.

Many ways to compute the standard error

Table: Regression of individual test scores on class size

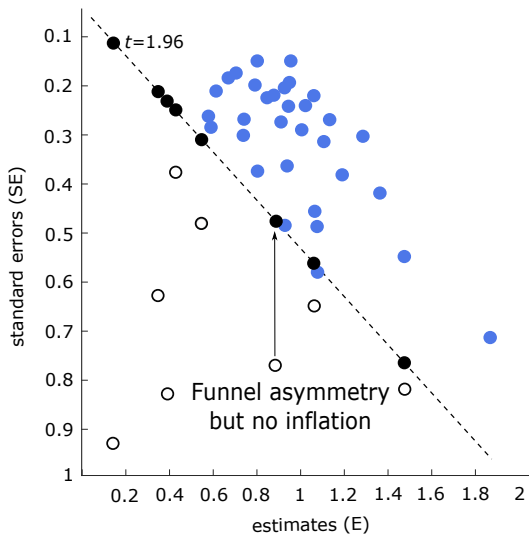
	Krueger (1999)	Replications using different computations of SE				
	(1)	(2)	(3)	(4)	(5)	(6)
		Bootstrap of class clusters	Class clusters	School clusters	Huber-White SE	Plain vanilla SE
Small class	4.82 (2.19)	4.71 (2.00)	4.71 (1.88)	4.71 (1.38)	4.71 (0.79)	4.71 (0.76)
Sample	5,861	5,743	5,743	5,743	5,743	5,743

Notes: Dependent variable: test score percentile. Standard errors (SE) in parentheses.

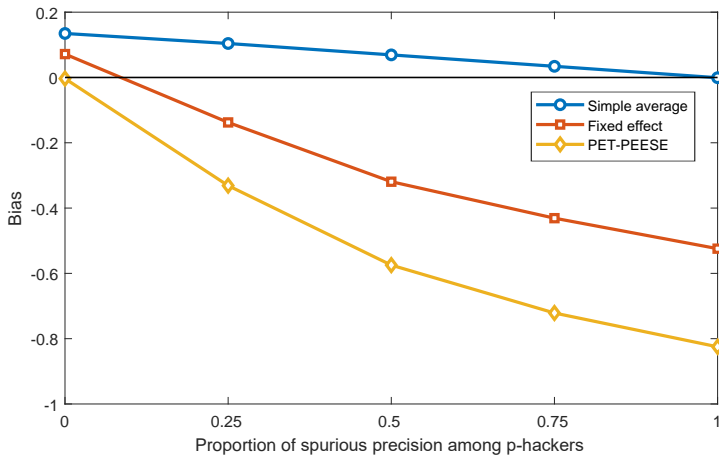
Meta-analysis of the class size effect

Available at meta-analysis.cz/class. Spoiler: effect size tiny.

Spurious precision



Repercussions: bias



Meta-Analysis Instrumental Variable Estimator

Take the PEESE regression without inverse-variance weights:

$$\hat{E}_i = E_0 + \beta SE(\hat{E}_i)^2 + v_i, \quad (1)$$

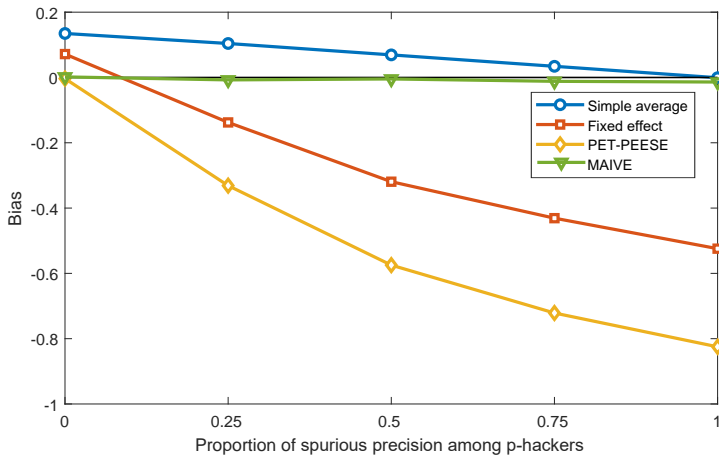
But instead of reported SE, use the portion of SE that can be explained by sample size [$\hat{\alpha}_0 + \hat{\alpha}_1(1/N_i)$]:

$$SE(\hat{E}_i)^2 = \alpha_0 + \alpha_1(1/N_i) + \pi_i, \quad (2)$$

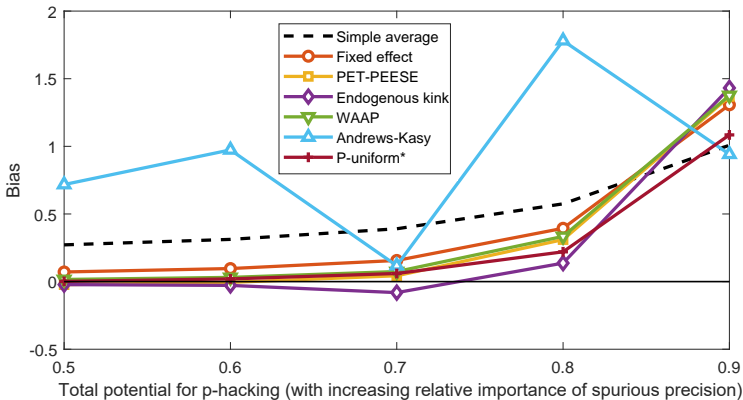
Why not simply replace SE^2 with $1/N$?

- 1 SE influenced by many things. More instruments possible.
- 2 N imperfect predictor of SE \rightarrow need correct meta SEs.
- 3 Replacement a special case of the instrumental approach.

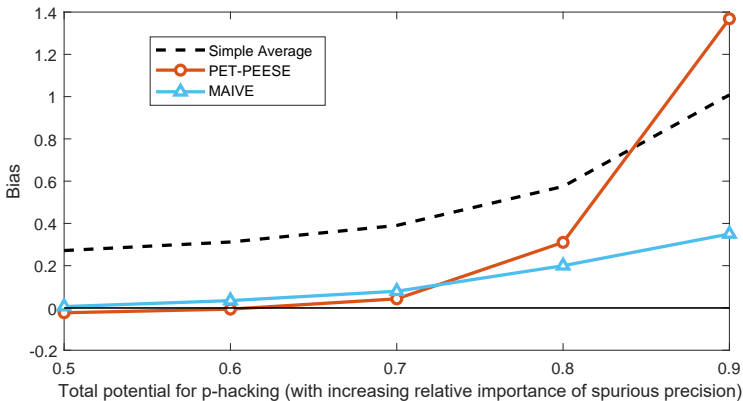
MAIVE solves the problem



Standard estimators still biased



MAIVE still works (but imperfectly)



Next steps

Working on (revision & sequel):

- 1 Add more complexities to simulations.
- 2 Check whether MAIVE helps explain differences between meta-analyses and multilab replications.
- 3 Compare the extent of spurious precision across fields.

Meta-research group in Prague

meta-analysis.cz

Our team's recent meta-analyses

-  Matousek, J., T. Havranek, & Z. Irsova (2022):
Individual Discount Rates: A Meta-Analysis of
Experimental Evidence.
Experimental Economics 25: 318-358.
-  Elminejad, A., T. Havranek, & Z. Irsova (2023):
Relative Risk Aversion: A Meta-Analysis.
meta-analysis.cz/risk
-  Cala, P., T. Havranek, Z. Irsova, J. Matousek (2023):
Financial Incentives and Performance: A Meta-Analysis of
Economics Evidence.
meta-analysis.cz/incentives